

## أدرب وأحل المسائل

### التكامل

أجد كلاً من التكاملات الآتية:

$$\int (x^2(2x^3+5))^4 dx \quad (1)$$

$$u=2x^3+5 \Rightarrow du=6x^2 dx \Rightarrow dx = \frac{du}{6x^2} \int x^2(2x^3+5)^4 dx = \int x^2 u^4 \times \frac{du}{6x^2} = \int \frac{1}{6} u^4 du = \frac{1}{6} \times \frac{u^5}{5} + C = \frac{1}{30} (2x^3+5)^5 + C$$

$$\int (x^2x+3) dx \quad (2)$$

$$u=x+3 \Rightarrow dx=du, x=u-3 \int (x^2x+3) dx = \int (u-3)^2 u du = \int (u^3 - 6u^2 + 9u) du = \frac{1}{4} u^4 - 2u^3 + \frac{9}{2} u^2 + C = \frac{1}{4} (x+3)^4 - 2(x+3)^3 + \frac{9}{2} (x+3)^2 + C = \frac{1}{4} (x+3)^4 - 2(x+3)^3 + \frac{9}{2} (x+3)^2 + C$$

$$\int (x(x+2))^3 dx \quad (3)$$

$$u=x+2 \Rightarrow dx=du, x=u-2 \int (x(x+2))^3 dx = \int (u-2)^3 u du = \int (u^4 - 2u^3 + 4u^2 - 8u) du = \frac{1}{5} u^5 - \frac{2}{4} u^4 + \frac{4}{3} u^3 - 4u^2 + C = \frac{1}{5} (x+2)^5 - \frac{1}{2} (x+2)^4 + \frac{4}{3} (x+2)^3 - 4(x+2)^2 + C$$

$$\int (x(x+4))^2 dx \quad (4)$$

$$u=x+4 \Rightarrow dx=du, x=u-4 \int (x(x+4))^2 dx = \int (u-4)^2 u du = \int (u^3 - 4u^2 + 16u) du = \frac{1}{4} u^4 - \frac{4}{3} u^3 + 8u^2 + C = \frac{1}{4} (x+4)^4 - \frac{4}{3} (x+4)^3 + 8(x+4)^2 + C$$

$$\int (2x \cos x) dx \quad (5)$$

$$x \Rightarrow dx = du - \sin x \Rightarrow du = -\sin x - 1 \Rightarrow dx = \frac{du}{-\sin x - 1} \int (2x \cos x) dx = \int \frac{2 \cos x (2x \cos x) dx}{-\sin x - 1} = \int \frac{4 \cos^2 x}{-\sin x - 1} dx = \int \frac{4(1 - \sin^2 x)}{-\sin x - 1} dx = \int \frac{4(1 - \sin x)(1 + \sin x)}{-\sin x - 1} dx = \int -4(1 - \sin x) dx = -4x + 4 \cos x + C$$

$$\int (e^{3x} e^{x+1}) dx \quad (6)$$

$$u=e^{x+1} \Rightarrow du=e^x dx \Rightarrow dx = \frac{du}{e^x} \int (e^{3x} e^{x+1}) dx = \int e^{3x} u \times \frac{du}{e^x} = \int e^{2x} u du = \int (u-1)^2 u du = \int (u^3 - 2u^2 + u) du = \frac{1}{4} u^4 - \frac{2}{3} u^3 + \frac{1}{2} u^2 + C = \frac{1}{4} (e^{x+1})^4 - \frac{2}{3} (e^{x+1})^3 + \frac{1}{2} (e^{x+1})^2 + C$$

$$\int x dx \quad (7) \sec^4 f$$

$$x \Rightarrow du dx = \sec x) dx u = \tan x (1 + \tan^2 x dx = \int \sec^2 x \times \sec^2 x dx = \int \sec^2 \sec^4 f$$

$$x = \int (1 + u^2) du = u + \frac{1}{3} u^3 + C = \tan x + \frac{1}{3} \tan^3 x + C = \tan$$

$$\int x dx \quad (8) x \cos^2 \tan f$$

$$x \int \tan x \Rightarrow dx = du \sec^2 x \Rightarrow du dx = \sec^2 x dx u = \tan x \sec^2 x dx = \int \tan x \cos^2 \tan f$$

$$x + C = \int u du = \frac{1}{2} u^2 + C = \frac{1}{2} \tan^2 x \times du \sec^2 x dx = \int u \sec^2 x \cos^2 n$$

$$\int x dx \quad (9) \ln \sin f$$

$$u du = -\cos u \times x du = \int \sin x) x dx = \int \sin(\ln x \Rightarrow du dx = \frac{1}{x} \Rightarrow dx = x du \int \sin u = \ln$$

$$x) + C (\ln u + C = -\cos$$

$$\int x dx \quad (10) x^1 + \sin^2 x \cos \sin f$$

$$x) + C (1 + \sin^2 x dx = \frac{1}{2} \ln x^1 + \sin^2 x \cos x dx = \frac{1}{2} \int 2 \sin x^1 + \sin^2 x \cos \sin f$$

$$\int (2e^x - 2e^{-x})(e^x + e^{-x})^2 dx \quad (11) f$$

$$u = e^x + e^{-x} \Rightarrow du dx = e^x - e^{-x} \Rightarrow dx = du e^x - e^{-x} \int 2e^x - 2e^{-x} (e^x + e^{-x})^2 d$$

$$x = \int 2(e^x - e^{-x}) u^2 \times du e^x - e^{-x} = \int 2u^2 - 2 du = -\frac{2}{3} u^3 + C = -\frac{2}{3} (e^x + e^{-x})^3 + C$$

$$\int x(x+1)^{x+1} dx \quad (12) - f$$

$$u = x+1 \Rightarrow dx = du, x = u-1 \int -x(x+1)^{x+1} dx = \int 1-u u^u du = \int 1-u u^3 du = \int$$

$$(u^3 - 3u^2 - u - 1) du = \frac{1}{4} u^4 - \frac{3}{3} u^3 - \frac{1}{2} u^2 - u + C = \frac{1}{4} (x+1)^4 - (x+1)^3 - \frac{1}{2} (x+1)^2 - (x+1) + C =$$

$$-\frac{1}{4} x^4 + \frac{1}{2} x^3 - \frac{1}{4} x^2 + \frac{1}{2} x + C$$

$$\int x(x+10)^3 dx \quad (13) f$$

$$u = x+10 \Rightarrow dx = du, x = u-10 \int x(x+10)^3 dx = \int (u-10) u^3 du = \int (u^4 - 10u^3$$

$$) du = \frac{1}{5} u^5 - 10 \frac{1}{4} u^4 + C = \frac{1}{5} (x+10)^5 - \frac{5}{2} (x+10)^4 + C = \frac{1}{5} (x+10)^5 - \frac{5}{2} (x+10)^4 + C$$

$$\int x^2 dx \quad (14) x^2 \tan^7 \sec^2) f$$

$$x^2 dx = \int \sec^2 x \tan^7 x^2 \int \sec^2 x^2 \Rightarrow dx = 2 du \sec^2 x^2 \Rightarrow du dx = 12 \sec^2 u = \tan x^2 + C x^2 = 2 \int u^7 du = 14 u^8 + C = 14 \tan^8 x^2 u^7 \times 2 du \sec^2$$

$$(x dx (15 x \sec x + e \sin \sec^3 \int$$

$$x x e \sin x dx + \int \cos x) dx = \int \sec^2 x e \sin x + \cos x dx = \int (\sec^2 x \sec x + e \sin \sec^3 \int x dx + x dx = \int \sec^2 x \sec x + e \sin x \int \sec^3 x \Rightarrow dx = du \cos x \Rightarrow du dx = \cos dx u = \sin x + C x + e \sin x + e u + C = \tan x + \int e u du = \tan x = \tan x e u \times du \cos \int \cos$$

$$(x dx (16 x^3) \cos^3 \sin + 1) \int$$

$$x dx = \int (1 + u^{13}) \cos^3 x^3) \cos^3 x \int (1 + \sin x \Rightarrow dx = du \cos x \Rightarrow du dx = \cos u = \sin x) du = \int (1 + u^{13}) (1 - u^2 x du = \int (1 + u^{13}) (1 - \sin^2 x = \int (1 + u^{13}) \cos^2 x du \cos) du = \int (1 + u^{13}) (1 - u^2) du = \int (1 - u^2 + u^{13} - u^7) du = u - \frac{1}{3} u^3 + \frac{34}{43} u^{43} - \frac{1}{31} u^{31} + C = \sin x + C x - \frac{1}{310} \sin^{103} x + \frac{34}{43} \sin^{43} x - \frac{1}{310} \sin^{310} x + C = \sin$$

$$(x dx (17 x \sec^5 \sin \int$$

$$x \int \sin x \Rightarrow dx = du - \sin x \Rightarrow du dx = -\sin x dx u = \cos x \cos - 5 x dx = \int \sin x \sec^5 \sin \int x + x = - \int u - 5 du = 14 u - 4 + C = 14 \cos - 4 x u - 5 \times du - \sin x dx = \int \sin x \sec^5 n x + C C = 14 \sec^4$$

$$(x dx (18 x \cos^3 x + \tan \sin \int$$

$$x + s x (\sec x \sec x) dx = \int \tan x \sec^3 x + \tan x \sec^2 x dx = \int (\tan x \cos^3 x + \tan \sin \int x dx \cos^3 x + \tan x \int \sin x \sec x \Rightarrow dx = du \tan x \sec x \Rightarrow du dx = \tan x) dx u = \sec^2 x = \int (u + u^2) du = \frac{1}{2} u^2 + \frac{1}{3} u^3 + C = \frac{1}{2} \sec^2 x \sec x (u + u^2) du \tan x \sec x = \int \tan x + C x + \frac{1}{3} \sec^3 x$$

أجد قيمة كلا من التكاملات الآتية:

$$(2 x dx (19 x^{1 - \cos 20\pi/4} \sin \int$$

$$|2 x^2 x = |\sin^2 x = \sin^2 \cos^2 - 1$$

لكن الزاوية  $2x$  تكون ضمن الربع الأول عندما  $0 < 2x < \pi/4$

لذا فإن  $2x > 0 \sin$  ويكون  $2x > 0 \sin$

$$x \Rightarrow x dx u = \sin x \cos 2x dx = \int_0^{\pi/4} 2 \sin 2x \sin 2x dx = \int_0^{\pi/4} 2 \sin^2 x dx = \int_0^{\pi/4} 2(1 - \cos 2x) dx = 2x - \sin 2x \Big|_0^{\pi/4} = 2 \cdot \frac{\pi}{4} - \sin \frac{\pi}{2} = \frac{\pi}{2} - 1$$

$$\int_0^{\pi/2} x^2 dx = \frac{1}{3} x^3 \Big|_0^{\pi/2} = \frac{1}{3} \left(\frac{\pi}{2}\right)^3 = \frac{\pi^3}{24}$$

$$x^2 dx = \int_0^{\pi/4} u = x^2 \Rightarrow du dx = 2x \Rightarrow dx = \frac{du}{2x} \quad x = \frac{\pi}{2} \Rightarrow u = \frac{\pi^2}{4} \quad x = 0 \Rightarrow u = 0$$

$$\int_0^{\pi/4} \pi^2 x \sin \pi^2 x dx = \int_0^{\pi^2/4} \frac{u}{2} \cos u du = \frac{1}{2} \int_0^{\pi^2/4} u \cos u du = \frac{1}{2} \left[ u \sin u + \cos u \right]_0^{\pi^2/4} = \frac{1}{2} \left( \frac{\pi^2}{4} \sin \frac{\pi^2}{4} + \cos \frac{\pi^2}{4} - 1 \right)$$

$$\int_0^1 (1+x^3)^2 dx = \int_0^1 (1+2x^3+x^6) dx = \left[ x + \frac{2}{4}x^4 + \frac{1}{7}x^7 \right]_0^1 = 1 + \frac{1}{2} + \frac{1}{7} = \frac{17}{14}$$

$$u = 1+x^2 \Rightarrow du dx = 2x \Rightarrow dx = \frac{du}{2x} \quad x^2 = u - 1 \quad x = 0 \Rightarrow u = 1 \quad x = 1 \Rightarrow u = 2$$

$$\int_0^1 (1+x^3)^2 dx = \int_1^2 (u-1)^2 \frac{du}{2(u-1)} = \frac{1}{2} \int_1^2 (u-1) du = \frac{1}{2} \left[ \frac{1}{2}u^2 - u \right]_1^2 = \frac{1}{2} \left( \frac{1}{2}(2^2) - 2 - \left( \frac{1}{2}(1^2) - 1 \right) \right) = \frac{1}{2} (2 - 2 - \frac{1}{2} + 1) = \frac{1}{4}$$

$$\int_0^{\pi/3} x \tan 50\pi/3 \sec^2 x dx = \frac{50\pi}{3} \int_0^{\pi/3} x \sec^2 x dx$$

$$x \tan x = 0 \Rightarrow u = 0 \quad x = \pi/3 \Rightarrow u = 3 \quad \int_0^{\pi/3} \pi^3 \sec^2 x dx = \int_0^3 \pi^3 \sec^2 u du = \pi^3 \tan u \Big|_0^3 = \pi^3 \tan 3$$

$$\int_0^2 (x-1)e^{(x-1)^2} dx = \frac{1}{2} \int_0^2 (x-1)e^{(x-1)^2} dx$$

$$u = (x-1)^2 \Rightarrow du dx = 2(x-1) \Rightarrow dx = \frac{du}{2(x-1)} \quad x = 0 \Rightarrow u = 1 \quad x = 2 \Rightarrow u = 1$$

$$\int_0^2 (x-1)e^{(x-1)^2} dx = \int_1^1 \frac{1}{2} e^u du = 0$$

$$\int_0^2 (x^2+1)^2 dx = \int_0^2 (x^4+2x^2+1) dx = \left[ \frac{1}{5}x^5 + \frac{2}{3}x^3 + x \right]_0^2 = \frac{32}{5} + \frac{16}{3} + 2 = \frac{192+160+60}{15} = \frac{412}{15}$$

$$u = 2+x \Rightarrow du dx = 1 \Rightarrow dx = du \quad x = 3 \Rightarrow u = 5 \quad x = 4 \Rightarrow u = 6$$

$$\int_3^4 (2+x)^2 dx = \int_5^6 u^2 du = \frac{1}{3} u^3 \Big|_5^6 = \frac{1}{3} (6^3 - 5^3) = \frac{1}{3} (216 - 125) = \frac{91}{3}$$

$$\int_0^1 10x(1+x^3)^2 dx = \frac{10}{3} \int_0^1 x(1+x^3)^2 dx$$

$$u = 1+x^3 \Rightarrow du dx = 3x^2 \Rightarrow dx = \frac{du}{3x^2} \quad x = 0 \Rightarrow u = 1 \quad x = 1 \Rightarrow u = 2$$

$$\int_0^1 10x(1+x^3)^2 dx = \int_1^2 \frac{10}{3} u^2 du = \frac{10}{9} u^3 \Big|_1^2 = \frac{10}{9} (2^3 - 1^3) = \frac{10}{9} (8 - 1) = \frac{70}{9}$$

$$\int_0^{\pi/6} x \sin 0\pi/6 \cos x dx = \int_0^{\pi/6} x \cos x dx$$

$$x=0 \Rightarrow u=1 \quad x=\pi/6 \Rightarrow u=3/2 \quad \int_0^{\pi/6} 2 \cos x \Rightarrow dx = du - \sin x \Rightarrow du dx = -\sin u = \cos 2u$$

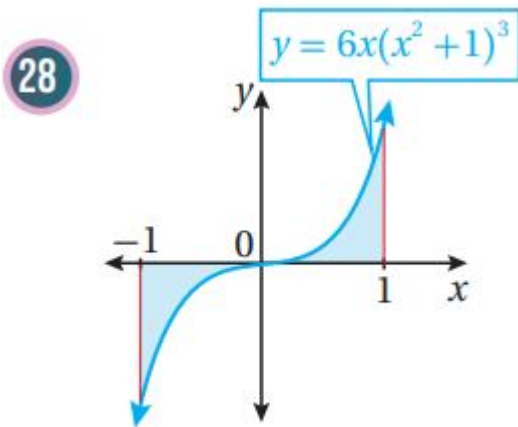
$$2 \int_{3/2}^2 \cos u du = -2 \ln |x| = -2 \ln |3/2| = -2 \ln 3/2 = -2(\ln 3 - \ln 2) \approx 0.256$$

$$\int_0^{\pi/2} x \cot x dx = \int_0^{\pi/2} x \frac{\cos x}{\sin x} dx = \int_0^{\pi/2} x \csc x dx$$

$$x=\pi/2 \Rightarrow u=0 \quad x=\pi/4 \Rightarrow u=1 \quad \int_{\pi/4}^{\pi/2} x \cot x dx \Rightarrow dx = du - \csc^2 x \Rightarrow du dx = -\csc^2 u = \cot u$$

$$x = \int_{10}^{-u} 5 du = -16u^6 |_{10} = 16xu^5 du - \csc^2 x dx = \int_{10}^{\csc^2 x} \cot^5 x dx$$

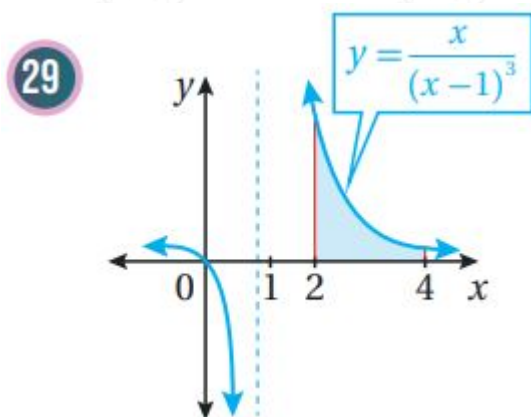
أجد مساحة المنطقة المظللة في كل من التمثيلات البيانية الآتية:



$$A = -\int_{-1}^0 6x(x^2+1)^3 dx + \int_0^1 6x(x^2+1)^3 dx \quad u = x^2+1 \Rightarrow du dx = 2x \Rightarrow dx = du/2x$$

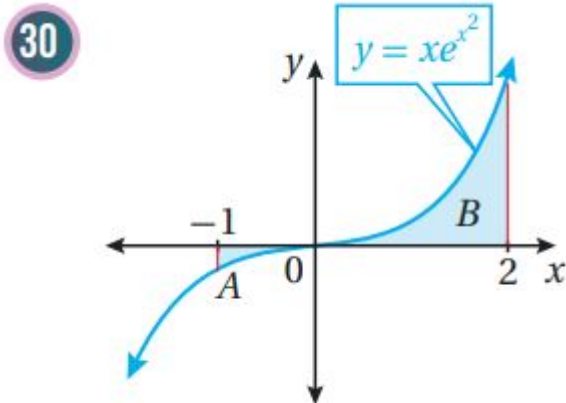
$$u^2 x x = -1 \Rightarrow u = 2x = 0 \Rightarrow u = 1 \quad x = 1 \Rightarrow u = 2 \quad A = -\int_2^1 3u^3 du + \int_1^2 3u^3 du$$

$$x = \int_{12}^3 u^3 du + \int_{12}^3 u^3 du = \int_{12}^6 u^3 du = 64u^4 |_{12} = 452$$



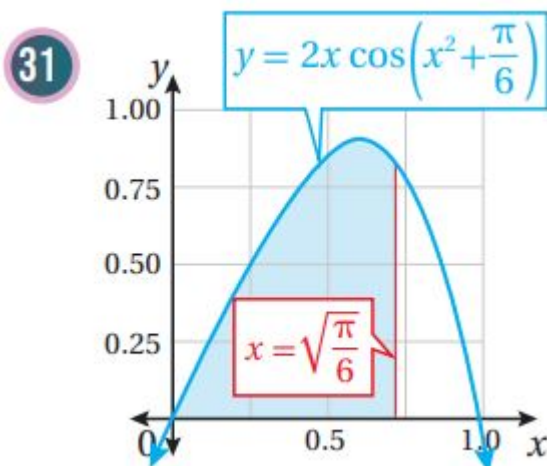
$$A = \int_2^4 \frac{x}{(x-1)^3} dx \quad u = x-1 \Rightarrow dx = du, x = u+1 \quad x=2 \Rightarrow u=1 \quad x=4 \Rightarrow u=3$$

$$A = \int_1^3 \frac{u+1}{u^3} du = \int_1^3 (u^{-2} + u^{-3}) du = (-u^{-1} - \frac{1}{2}u^{-2}) |_{13} = -\frac{1}{3} - \frac{1}{2}(\frac{1}{9}) + 1 + \frac{1}{2} = 109$$



$$u = x^2 \Rightarrow \frac{du}{dx} = 2x \Rightarrow dx = \frac{du}{2x} \Rightarrow \frac{dx}{x} = \frac{du}{2u} \Rightarrow \int \frac{dx}{x} = \frac{1}{2} \int \frac{du}{u} \Rightarrow \ln|x| = \frac{1}{2} \ln|u| \Rightarrow \ln|x| = \frac{1}{2} \ln|x^2| \Rightarrow \ln|x| = \ln|x|$$

$$A = \int_{-1}^0 x e^{x^2} dx + \int_0^2 x e^{x^2} dx = \int_{-1}^0 \frac{1}{2} e^u du + \int_0^2 \frac{1}{2} e^u du = \frac{1}{2} [e^u]_{-1}^0 + \frac{1}{2} [e^u]_0^2 = \frac{1}{2} (e^0 - e^{-1}) + \frac{1}{2} (e^2 - e^0) = \frac{1}{2} (1 - e^{-1} + e^2 - 1) = \frac{1}{2} (e^2 - e^{-1}) \approx 27.658$$



$$u = x^2 + \frac{\pi}{6} \Rightarrow \frac{du}{dx} = 2x \Rightarrow dx = \frac{du}{2x} \Rightarrow \frac{dx}{x} = \frac{du}{2u} \Rightarrow \int \frac{dx}{x} = \frac{1}{2} \int \frac{du}{u} \Rightarrow \ln|x| = \frac{1}{2} \ln|u| \Rightarrow \ln|x| = \frac{1}{2} \ln|x^2 + \frac{\pi}{6}|$$

$$A = \int_0^{\sqrt{\pi/6}} 2x \cos(x^2 + \frac{\pi}{6}) dx + \int_{\sqrt{\pi/6}}^1 2x \cos(x^2 + \frac{\pi}{6}) dx = \int_{\pi/6}^{\pi/3} \cos u du + \int_{\pi/3}^{\pi/2} \cos u du = [\sin u]_{\pi/6}^{\pi/3} + [\sin u]_{\pi/3}^{\pi/2} = (\sin \frac{\pi}{3} - \sin \frac{\pi}{6}) + (\sin \frac{\pi}{2} - \sin \frac{\pi}{3}) = (\frac{\sqrt{3}}{2} - \frac{1}{2}) + (1 - \frac{\sqrt{3}}{2}) = 3 - \sqrt{3} \approx 0.366$$

في كل مما يأتي المشتقة الأولى للاقتران  $(f(x), g(x))$ ، ونقطة يمر بها منحنى  $y = f(x)$ .  
أستعمل المعلومات المعطاة لإيجاد قاعدة الاقتران  $(f(x), g(x))$ :

(32)  $f(x) = 2x(4x^2 - 10)^2; (2, 10)$

$$f(x) = \int f'(x) dx = \int 2x(4x^2 - 10)^2 dx \quad u = 4x^2 - 10 \Rightarrow \frac{du}{dx} = 8x \Rightarrow dx = \frac{du}{8x} \Rightarrow \int \frac{2x}{8x} u^2 du = \int \frac{1}{4} u^2 du = \frac{1}{12} u^3 + C \Rightarrow f(x) = \frac{1}{12} (4x^2 - 10)^3 + C$$

$$f(2) = \frac{1}{12} (216) + C = 10 \Rightarrow C = -8 \Rightarrow f(x) = \frac{1}{12} (4x^2 - 10)^3 - 8$$

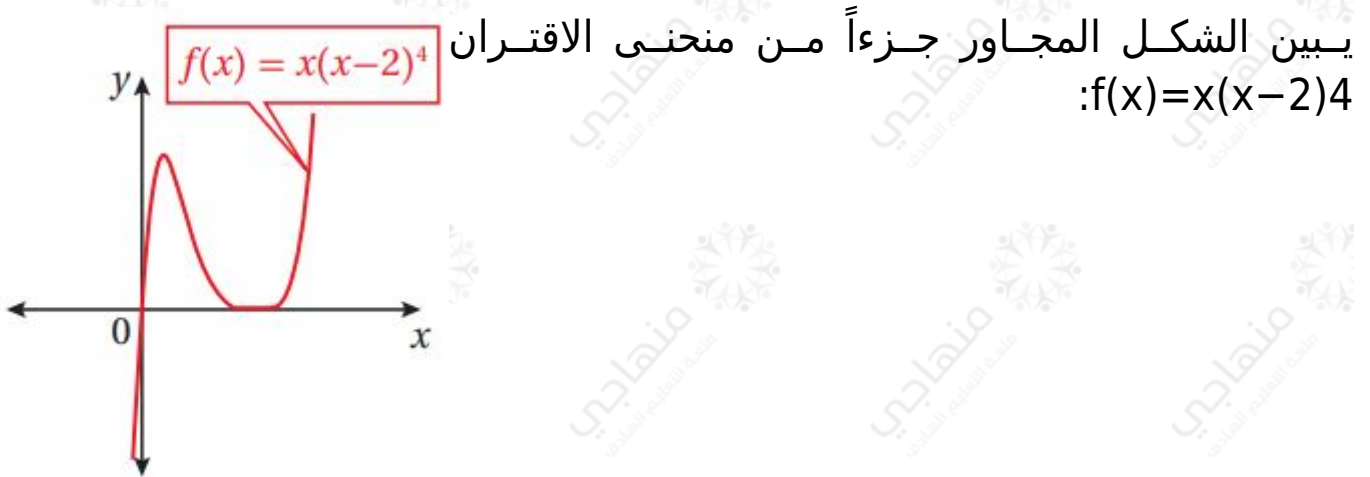
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$$(f'(x) = x^2 e^{-0.2x^3}; (0, 32)) \quad (33)$$

$$f(x) = \int f'(x) dx = \int x^2 e^{-0.2x^3} dx \quad u = -0.2x^3 \Rightarrow du/dx = -0.6x^2 \Rightarrow dx = du / -0.6x^2$$

$$x^2 f(x) = \int x^2 e^u du / -0.6x^2 = -1/0.6 \int e^u du = -5/3 e^u + C \Rightarrow f(x) = -5/3 e^{-0.2x^3} + C$$

$$+ C f(0) = -5/3 + C 32 = -5/3 + C \Rightarrow C = 196 \Rightarrow f(x) = -5/3 e^{-0.2x^3} + 196$$



(34) أجد إحداثي نقطة تماس الاقتران مع المحور x

نجد أصفار الاقتران بحل المعادلة  $f(x) = 0$

$$x(x-2)^4 = 0 \Rightarrow x = 0, x = 2$$

نقطة التقاطع  $(0, 0)$ , فتكون نقطة التماس  $(2, 0)$

ويمكن التحقق بحساب  $f'(2)$ :

$$f'(x) = (x-2)^4 + 4x(x-2)^3 \quad f'(2) = (2-2)^4 + 4(2)(2-2)^3 = 0$$

(35) أجد مساحة المنطقة المحصورة بين منحنى الاقتران  $f(x)$  والمحور x

$$A = \int_0^2 x(x-2)^4 dx \quad u = x-2 \Rightarrow dx = du, x = u+2 \quad x=0 \Rightarrow u = -2 \quad x=2 \Rightarrow u = 0$$

$$A = \int_{-2}^0 (u+2)u^4 du = \int_{-2}^0 (u^5 + 2u^4) du = (1/6 u^6 + 2/5 u^5) \Big|_{-2}^0$$

$$= 0 - (1/6 (-2)^6 + 2/5 (-2)^5) = 32/15$$

(36) يتحرك جسيم في مسار مستقيم، وتعطى سرعته المتجهة بالاقتران:

$\omega t \cos 2v(t) = \sin$  حيث t الزمن بالثواني، و v سرعته المتجهة بالمتري لكل ثانية،

و  $b$  ثابت، إذا انطلق الجسم من نقطة الأصل، فأجد موقعه بعد  $t$  ثانية.

$$wts(t) = wt \Rightarrow dt = du - w \sin wt \Rightarrow dudx = -w \sin wt dt u = \cos wt \cos 2s(t) = f \sin wt + Cwt = -1w \int u^2 du = -13wu^3 + C \Rightarrow s(t) = -130 \cos 3wt u^2 du - w \sin f \sin$$

لكن  $s(0) = 0$  لأن الجسم انطلق من نقطة الأصل.

$$wt + 13ws(0) = -13w + C0 = -13w + C \Rightarrow C = 13w \Rightarrow s(t) = -13w \cos 3$$



(37) طب: يمثل الاقتران  $C(t)$  تركيز دواء في الدم بعد  $t$  دقيقة من حقنه في جسم مريض، حيث  $C$  مقيسة بالمليغرام لكل سنتيمتر مكعب ( $mg/cm^3$ )، إذا كان تركيز الدواء لحظة حقنه في جسم المريض  $0.5 mg/cm^3$ ، وأخذ يتغير بمعدل  $C'(t) = -0.01e^{-0.01t}(1+e^{-0.01t})^2$ ، فأجد  $C(t)$ .

$$C(t) = \int C'(t) dt = \int -0.01e^{-0.01t}(1+e^{-0.01t})^2 dt u = 1+e^{-0.01t} \Rightarrow du dt = -0.01e^{-0.01t} \Rightarrow dt = du - 0.01e^{-0.01t} C(t) = \int -0.01e^{-0.01t} u^2 \times du - 0.01e^{-0.01t} = \int u^2 du = -u^{-1} + K$$

استعمل الرمز  $K$  لثابت التكامل بدل  $C$  المعتاد لتمييز ثابت التكامل عن رمز الاقتران  $C$ :

$$C(t) = -(1+e^{-0.01t})^{-1} + K C(0) = -(2)^{-1} + K12 = -12 \Rightarrow K = 1 \Rightarrow C(t) = -(1+e^{-0.01t})^{-1} + 1 C(t) = -11 + e^{-0.01t} + 1$$

(38) أجد قيمة  $\int \ln \ln x dx$ ، ثم اكتب الإجابة بالصيغة الآتية:  $dab + c \ln$ ، حيث  $a, b, c, d$  ثوابت صحيحة.

$$3-2 = 3-2 = 1x = |3 \Rightarrow u = e \ln u = e^x - 2 \Rightarrow du dx = e^x \Rightarrow dx = du e^x e^x = u + 2x = \ln 4e^4 x e^x - 2 dx = \int 12e^4 x u du e^x = \int 12e^3 x u du 3 \ln 4 - 2 = 4 - 2 = 2 \int \ln 4 \Rightarrow u = e \ln u = \int 12(u+2)^3 u du = \int 12(u^3 + 6u^2 + 12u + 8) du = \int 12(u^3 + 6u^2 + 12u + 8) du |u|^{12} = (13u^3 + 3u^2 + 12u + 8 \ln$$

(39) إذا كان:  $xf'(x) = \tan$ ، وكان:  $f(3) = 5$ ، فأثبت أن  $f(x) = \ln |\cos x| + 53 \cos$ .

$$3 + C5 = -\ln |\cos x| + C f(3) = -\ln |\cos x dx = -\ln x \cos x dx = -\int -\sin f(x) = \int \tan$$



$$x|+53\cos|\cos3|=\ln|\cos x|+5+\ln|\cos 3|f(x)=-\ln|\cos 3|+C\Rightarrow C=5+\ln|\cos$$